On the Limits of Causal Modeling:
Spatially-Structurally Complex Biological Phenomena

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Abstract
This paper examines the adequacy of causal graph theory as a tool for modeling biological phenomena. I argue that the causal graph approach reaches its limits when it comes to modeling biological phenomena that involve complex spatial and chemical-structural relations. Using a case study from molecular biology, I show why causal graph models fail to adequately represent and explain biological phenomena of this kind. The inadequacy of these models is due to their failure to include relevant spatial-structural information in a way that does not render the models non-explanatory, unmanageable, or inconsistent with basic assumptions of causal graph theory.

Acknowledgments
This paper arose from a collaboration with Marcel Weber during my time at the University of Geneva and it profited much from our stimulating discussions. I also thank Benjamin Jantzen, Christopher Hitchcock, Lorenzo Casini, Alexander Gebharter, Maximilian Huber, and the members of my DFG Research Group “Causation and Explanation” for their helpful comments on earlier versions of the paper. This material is based upon work supported by the German Research Foundation (DFG; FOR 1063).
1. Introduction

In recent decades, major advances have been made in formalizing causation and causal inference (Spirtes et al. 2000; Pearl 2000) and in using these formalisms to address traditional philosophical issues such as the nature of scientific explanation (Woodward 2003, Woodward and Hitchcock 2003). At the heart of these formal theories lie causal models that involve elements such as causal graphs, probability distributions, Bayesian nets, and structural equations. Causal models are appreciated because they allow for inferring causal relations from observed probabilistic correlations and for predicting the effects of manipulations and interventions, and because they can be used for representing and explaining causal relationships in very general, formal terms.

Proponents of the causal modeling approach usually emphasize and exemplify the wide scope of this approach, for instance, by demonstrating its applicability to mechanistic explanations in biology and medicine (Casini et al. 2011; Clarke et al. 2014; Gebharter and Kaiser 2014). Similarly, Woodward’s interventionist theory of causation and causal explanation (2003), which makes extensive use of causal graphs, is supposed to be applicable to a wide range of causal relationships, including those in the biological realm (2011, 2013).

In this paper, I agree that causal modeling is a powerful approach to formally represent, explain, and discover causal relations. However, I also think that its scope should not be overestimated and that it is important to also recognize the limits of the causal modeling approach. This paper explicates one of these limits: the explanation of spatially and structurally complex biological phenomena. Based on the analysis of a case study from molecular biology, protein-DNA recognition, I show that the formal tools of causal graph theory are too limited to offer adequate causal explanations of the biological phenomena that essentially involve complementarity of chemical structures, spatial fit between protein and DNA, DNA deformations.

Interestingly, Woodward has basically conceded this point, but he does not see this as a limitation of his causal modeling or interventionist approach to scientific explanation. Taking a relaxed stance, he argues that complex spatiotemporal information can just be added to the backbone of causal difference-making information and can be used to “organize” (2011, 423) or “fine-tune” (2013, 55) it. This paper shows that things are not that easy. Some biological processes involve complex spatial and structural relations that are central to explaining these processes but that cannot be represented in causal graph models without rendering the model un-explanatory, unmanageable, or contradictory. To be clear: This is not a claim about biological practice, for instance the claim that biologists wrongly use causal graphs to model certain phenomena. Rather, the purpose of this paper is primarily philosophical. Given the increased popularity of causal modeling approaches, it is important to recognize not only their strengths but also their limits: Which kinds of

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1 Other limitations are that causal graph models provide a confusing and ontologically inadequate view of the entities and activities constituting mechanisms (Gebharter and Kaiser 2014) and that they fail to account for the complex dynamics of biological phenomena (Weber 2016).
causal phenomena studied in biology cannot be explained by means of causal graphs and why is this so?

I proceed as follows. Section 2 briefly reviews the core notions and assumptions made in the causal modeling literature. In Section 3, I introduce my case study and carve out three kinds of information that any adequate explanatory model of protein-DNA recognition must include. Section 4 meets an important objection that challenges the overall project of this paper and thereby clarifies the causal character of the explanation of protein-DNA recognition. I then construct a causal graph model of protein-DNA recognition (Section 5), discuss different ways of including spatial-structural information into the model, and argue that each modeling strategy fails to yield an adequate explanation of the phenomenon (Section 6).

2. Causal Modeling

Causal models can be grouped into two kinds: causal Bayesian networks and structural equation models. For the purposes of this paper, I focus on causal Bayesian networks (also called causal graph models) and leave structural equations aside. Causal graph models combine mathematics and philosophy: the mathematical elements are directed acyclic graphs (DAGs) and probability theory, the philosophical elements are assumptions about the relationship between causation and probability (Spirtes et al. 2000).

A directed acyclic graph (DAG) is an ordered pair \( G = \langle V, E \rangle \), where \( V \) is a set of variables and \( E \) is a set of directed edges (graphically represented by arrows). A variable can be binary, its values representing, for instance, the instantiation or non-instantiation of some property, or can have multiple values or even be continuous.

Besides the DAG, a causal model consists of a probability distribution \( P \) that assigns a real number \( 0 \geq r \geq 1 \) to every value combination of variables in \( V \) such that the sum of all assigned \( r \) equals 1. The pair of DAG \( G \) and probability distribution \( P \) over \( V \) is referred to as a Bayesian network if and only if \( G \) and \( P \) satisfy the Markov Condition. A DAG becomes a causal graph as soon as its edges are interpreted causally: an edge leading from variable \( X_1 \) to variable \( X_2 \) is interpreted such that \( X_1 \) is a direct cause of \( X_2 \). When DAGs are interpreted causally, the Markov Condition is assumed to be the correct connection between causal structure and probabilistic independence. This assumption is called the Causal Markov Condition (CMC): A directed acyclic graph \( G \) and a probability distribution \( P \) over variable set \( V \) satisfy CMC iff every variable \( X \) in \( V \) is probabilistically independent of \( X \)'s non-descendants given \( X \)'s parents (i.e., \( \text{INDEP}_{Pr}(X, \text{N-Des}(X) | \text{Pa}(X)) \)). CMC captures the intuition that conditioning on all common causes and on intermediate causes breaks down the probabilistic influence between two formerly correlated variables. Since causal models satisfy CMC, they allow for probabilistic prediction and manipulation.

3. Protein-DNA Recognition

Proteins that recognize and bind to specific DNA sequences are crucial to many biological processes. As transcription factors (TFs), they regulate gene transcription and thereby control processes such as cell differentiation. It is essential for the functioning of TFs that
they recognize and bind selectively to only one, or just a few, specific DNA sequences out of the millions present in a genome. Understanding this specificity of protein-DNA recognition and binding is of considerable theoretical and practical importance.

Current biological research on protein-DNA recognition and binding is multifaceted. Among the different aspects that researchers study are the following:

1. **Binding Sites Detection**: Where in the genome are protein-binding sites located? Which DNA sequence does a particular TF bind? (e.g., Cai and Huang 2012)

2. **Affinity/Specificity Measurements**: How do the binding affinities of a TF vary for different sequences? How is the specificity of a TF measured? (e.g., Stormo and Zhao 2010)

3. **Structure Determination**: What is the structure of a DNA-protein complex? Which structural motifs do TFs use to bind to the DNA? (e.g., Harrison 1991)

4. **Recognition Mechanism Identification**: How does a TF recognize its specific binding site? What are the mechanisms by which a TF reads out the DNA? (e.g., Rohs et al. 2010; Strauch 2001).

In this paper, I focus on the fourth set of questions and examine whether causal graph theory is an adequate tool for modeling mechanisms of protein-DNA recognition, without claiming that there must be a single model that captures all the different aspects of protein-DNA recognition and binding that are investigated in biological practice. To assess whether causal graph theory can be applied to mechanisms of protein-DNA recognition, I will first examine how biologists model and mechanistically explain how a TF recognizes its specific binding site. The aim of analyzing explanatory practice in biology is to reveal the kinds of information that are relevant to explaining this phenomenon and that thus must be included in any explanatory model of how protein-DNA recognition works.

Understanding the mechanisms of protein-DNA recognition has a long history. Initially, X-ray crystallography was used to uncover the structure of protein-DNA complexes (e.g., Pavletich and Pabo 1991). Crystallographic studies revealed that the surface of the DNA – in particular, its major groove – presents a distinctive pattern of hydrogen bond donors and acceptors and hydrophobic patches and that this pattern is recognized by a complementary set of donors and acceptors presented by the amino acid side chains of a TF. In other words, the TF recognizes the unique chemical signatures of the DNA bases of its binding site because its amino acids form a set of hydrogen bonds and hydrophobic contacts with the DNA bases. The specificity is conveyed not only through the number and kind of bonds formed but also through the uniqueness of the bonding geometry. These mechanisms of protein-DNA recognition are now commonly referred to as **direct readout** or “base readout” (Rohs et al. 2010, 233).

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2 The list is not exhaustive and there are interconnections between different questions (e.g., the structure of a TF will co-determine its plausible recognition mechanism).

3 The conditions under which mechanistic models of protein-DNA recognition are explanatory cannot simply be read off biological practice but must be critically reconstructed from it. This process involves also normative dimensions (Kaiser 2015, Chapter 2).
It was soon realized that the story is more complex than this because there is no one-to-one correspondence between DNA and protein sequences. For most TFs, the direct readout of base pairs through hydrogen bonds is thus not sufficient to explain their specificity. TFs recognize not only the chemical structure but also the shape of their DNA binding site. Depending on its sequence, DNA conformation can deviate from idealized B-DNA in various ways, each of which can be recognized by certain TFs. One of these ways is for the overall cylindrical shape of the DNA double-helix to be deformed. For example, the DNA can be gradually bent, which can position elements of the DNA backbone such that these otherwise non-specific contacts can become highly specific (Figure 1a). Another of these ways is for the geometry of the DNA to vary locally, for example, for the minor groove to be narrowed or the DNA to possess a kink. Minor groove narrowing typically enhances negative electrostatic potential, which then can be read by TFs (Figure 1c/d). Local kinks promote DNA conformations that optimize protein-DNA and protein-protein contacts (Figure 1b). Recognition mechanisms such as these are called indirect readout or “shape readout” (Rohs et al. 2010, 233).

![Bend](image)

**Bend**

![Kink](image)

**Kink**

![Narrow minor groove](image)

**Narrow minor groove**

![Narrow minor groove electrostatics](image)

**Narrow minor groove electrostatics**

Fig. 1: Examples of shape readout mechanisms (Rohs et al. 2010, Fig. 2)

In sum, biologists explain how a particular TF recognizes its specific binding site by describing the direct and indirect readout mechanisms that the TF combines to achieve the specificity required for its correct functioning. This explanation not only involves specifying the linear sequences of DNA and TF binding sites and revealing their complementarity by identifying the contacts that are made between bases and amino acids.
It also requires describing their bonding geometry and how DNA and TF spatially fit, how the conformation of the DNA deviates from idealized B-DNA, and how this deviation facilitates further protein-DNA contacts.

I conclude that three kinds of information are relevant to explaining how protein-DNA recognition works:

1. **Binding information** about the kinds of bonds that are formed between amino acid residues and DNA base-pairs (direct contacts), and about the parts of the DNA and the TF that indirectly interact with each other (indirect contacts);

2. **Chemical-structural information** about the primary sequences of DNA and TF binding sites, about the complementarity of their chemical structures;

3. **Spatial information** about the conformations of DNA and the TF and why they spatially fit, about how the DNA shape contributes to recognition.

Information of all three kinds is essential to explaining any mechanism of protein-DNA recognition because all three factors – causal interactions, chemical structural relations, and spatial relations – are all crucial to the working of these mechanisms. Understanding how a TF recognizes a specific DNA sequence (out of the millions present in the genome) requires knowing how the TF reads out the chemical structure of the DNA binding site, how the two molecules spatially fit together, and how the structural complementarity and spatial fit enable specific bonds to be formed. Hence, any explanatory model of protein-DNA recognition is adequate only if it includes all three kinds of information.

4. **Just a Matter of Non-causal Explanation?**

Before I start modeling the phenomenon of protein-DNA recognition by means of causal graphs, this section addresses a possible objection and thereby further clarifies the main claim of the paper. One might object that I am accusing causal graph theory of not being able to do something that it was never intended to do, namely represent non-causal explanations such as the explanation of how a particular protein recognizes its specific binding site. My response to this objection is threefold.

First, I do not agree that explanations of protein-DNA recognition are non-causal. Describing the recognition mechanisms that are at work in a particular case includes also specifying which functional groups of the DNA and the protein interact with each other to form certain kinds of bonds. The formation of chemical bonds, however, clearly is a causal process, which is why the explanation of protein-DNA recognition will be, at least partially, also causal.

Second, granted that binding information is information about causal relations, an opponent might still insist that the rest of the explanation represents non-causal relations, namely chemical structures, shapes, and spatial relations. Since causal graph theory was designed to represent causal dependencies only, so the opponent, why should one care about the news that these non-causal relations cannot be adequately represented in a causal graph model? One possible response to this objection is to point to the fact that philosophers actually are interested in this question. Whether non-causal relations such as supervenience or constitution relations can be represented in causal graph models or can be
dealt with in an interventionist framework is controversially discussed (e.g., Casini et al. 2011; Gebharter and Kaiser 2014; Woodward 2015; Baumgartner and Gebharter 2015). Thus, why not extend this discussion to other kinds of non-causal relations that play a central role in biological mechanisms?

Third, another, stronger response is to challenge the assumption that chemical-structural and spatial information are non-causal. According to many theories of causation, the shapes of DNA and the TF and the complementarity of their chemical structures turn out to be causes of the TF binding to DNA. In counterfactual terms, the complementarity of the chemical structures of DNA and the TF is a cause of the binding because if the chemical structures were not complementary, DNA and the TF would not bind. In an interventionist framework, for example, the bending of the DNA is a cause of the binding of a particular TF to the DNA because there is an ideal intervention such that if I intervene in the shape of the DNA and remove its bending, I will prevent the binding. Likewise, the 3-dimensional conformation of the TF typically makes a difference to the binding and, thus, is a cause of it. But if much of the chemical-structural and spatial information describes causes, then the question of this paper seems to be even more pressing: Is there a way to include this causal information into a causal graph model? Can causal graph theory be used to model and explain spatially-structurally complex biological phenomena such as protein-DNA recognition, or does it reach its limits?

5. How to Model Protein-DNA Recognition by Causal Graphs

How can we construct a formal causal model of the mechanisms by which a TF recognizes its specific DNA binding site? What happens before the recognition is that the TF diffuses into the nucleus, establishes some non-specific electrostatic interactions with the DNA backbone, which allows it to slide along the DNA (Strauch 2001), and finally encounters the DNA binding site in proper orientation. If recognition then occurs, it results in the binding of the TF to the DNA.

This causal chain of events (diffusion → non-specific interactions → encountering → binding) is useful in understanding the causal context of the recognition process, but it does not explain how recognition itself occurs and how it ensures the specificity of the binding. As I pointed out in Section 3, the latter requires, for instance, specifying which functional groups of the TF and the DNA encounter each other and which kinds of chemical bonds are formed. This binding information can be captured in a causal graph model not by introducing single variables for the encountering (E) and binding (B) of the TF and DNA, but rather by introducing fine-grained variables that represent sub-events, such as the encountering of a certain region of the protein with a certain region of the DNA (E₁,E₂...,Eₙ) and the formation of a certain kind of bond between a functional group of the protein and another of the DNA (B₁,B₂...,Bₙ). The resulting causal graph model M₁ is depicted in Figure 2.

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4 In contrast, proponents of a production theory of causation might argue that shapes and chemical structures of the TF and DNA are only constraints but not causes of their binding.
In its simplest version, the variables in M1 are binary variables, representing events such as “TF diffuses into nucleus” \((D)\), “non-specific electrostatic interactions between TF and DNA backbone” \((N)\), “a certain region of TF encounters a certain region of DNA binding site” \((E_n)\), and “formation of two hydrogen bonds between amine-residue of lysine25 and the carbonyl- and pyridyl-group of DNA base guanine26” \((B_2)\). As binary variables, each of them can take one of the two values “taking place” and “not taking place”. Alternatively, they might be interpreted as quantitative variables. \(D\) and \(N\) would then stand for the number or concentration of particular TFs diffusing into the nucleus and non-specifically interacting with the DNA backbone; \(E_1,E_2,\ldots,E_n\) and \(B_1,B_2,\ldots,B_n\) would stand for the number of encounterings and bond formations of the respective kinds. The arrows between the variables represent \(D\) being a direct cause of \(N\), which is a direct cause of \(E_1,E_2,\ldots,E_n\), which are direct causes of \(B_1,B_2,\ldots,B_n\). The “+” stands for a positive causal influence: raising the probability that \(N\) takes a high value raises the probability that, for example, \(E_3\) takes a high value. Since the binding of an amino acid residue to a nucleotide base may raise the probability that another bond is established, the causal graph model also contains arrows between the \(B\)-variables (e.g., the arrow between \(B_1\) and \(B_2\)).

6. Where the Limits of Causal Graph Models Lie

The causal graph model M1 succeeds in representing binding information. Explaining how a TF recognizes a specific DNA sequence out of the millions present in a genome, however, not only requires specifying the chemical bonds that are formed. It also requires elucidating the shapes of the TF and DNA, how they spatially fit, and how DNA conformation enables certain other interactions to occur \((spatial\ information)\); and it requires revealing the complementarity of the chemical structures of the TF and DNA \((chemical-structural\ information)\). The latter two kinds of information, however, are missing in M1.

The causal modelers might agree with me at this point and concede the inadequacy of M1. But they might insist that it is possible to render M1 adequate by including the missing explanatorily relevant spatial and chemical-structural information. I see two major
modeling strategies one could pursue. In what follows, I successively explain them and show why both fail to yield adequate explanations of protein-DNA recognition.5

One option is to include the missing spatial and chemical-structural information into the characterization of the variables $E_1, E_2, ..., E_n$ and $B_1, B_2, ..., B_n$. For instance, one could characterize $B_{12}$ not only as “formation of two hydrogen bonds between amine-residue of lysine$_{25}$ and the carbonyl- and pyridyl-group of DNA base guanine$_{26}$” but add “… where the lysine$_{25}$ residue is covalently bound to serine$_{17}$ residue and leucine$_{39}$ residue, forms a salt bridge to arginine$_{9}$ residue, has a close distance to DNA bases cytosine$_{28}$ and guanine$_{42}$, etc.”.

This strategy encounters three problems. First, storing complex spatial and structural information into the characterization of the variables renders $M_1$ unmanageable because the measurement of the values of the variables becomes very complicated or even unfeasible in practice. This is a problem for causal models of this phenomenon in general, not a problem that pertains to explanation in particular. Second, the strategy results in a causal model in which the spatial and structural information is highly fragmented because information about the shapes of the TF and DNA, their spatial orientation to each other, the effect of DNA conformation on interactions between the TF and DNA, the chemical structures of the TF and DNA, and their complementarity is distributed over the variables $E_1, E_2, ..., E_n$ and $B_1, B_2, ..., B_n$. This fragmentation is devastating to the explanatory power of the causal model since the resulting model fails to elucidate how spatial and chemical-structural relations contribute to the specificity of the recognition process (e.g., that TF and DNA spatially fit together and that DNA deformation enables specific interactions between the two macromolecules). Third, the modeling strategy gives rise to a causal model in which a great deal of the explanatorily relevant information is contained in the characterization of the variables, and not in the causal graphs that represent causal dependency relations. This suggests that the causal graphs are less informative and bear less explanatory weight than the characterization of the variables. But this seems to conflict with the typical way of conceiving causal graph models and reinforces the impression that one tries to add something that does not really fit.

A second option is to add to the causal model one or more variables that are supposed to represent the spatial and chemical-structural information. One could, for instance, add the variable $S$ that stands for the TF and DNA having certain conformations and chemical structures, the TF being oriented towards the DNA such that certain amino acid residues encounter certain DNA bases, the sequences of the TF and DNA being complementary. The resulting causal model $M_2$ is depicted in Figure 3.

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5 I am not providing a strict impossibility argument here because I can only discuss those modeling strategies that seem most important and obvious to me.
M2 accounts for the fact that whether or not a certain amino acid residue of the TF forms bonds to a certain DNA base depends not only on whether a particular TF region encounters the DNA binding site but also on whether the TF and DNA shapes enable the encountering in the first place (which is captured in Figure 3 by the arrow from $S$ to $E_2$), on whether TF and DNA structures are complementary, and on whether DNA deformation affects the binding (represented in Figure 3 by the arrows from $S$ to $B_1$ and $B_n$).

Despite these advantages, the revised causal model M2 is still not satisfactory. First, it has the feel of putting the missing relevant spatial and chemical-structural information in “by hand”: something that does not smoothly, automatically fit must be added under additional, atypical efforts. What reinforces this feeling is that all different spatial and chemical-structural information is represented by a single variable. It would be more adequate to add different variables ($S_1, S_2, \ldots, S_n$) for the TF conformation, the DNA shape, the spatial orientation of the TF towards DNA, the amino acid sequence of the TF, the chemical structure of the DNA binding site, and the complementarity of the TF and the DNA structures. These different variables could also be quantitative variables that represent, for instance, relative distances among sets of TF molecules and sets of DNA molecules. But this modeling strategy encounters the problem that the variables are no longer conceptually independent of each other, which violates a central requirement of causal graph theory. For example, because a specific TF conformation ($S_3$) requires a specific amino acid sequence ($S_5$), a change in the value of $S_5$ will simultaneously change the value of $S_3$. Likewise, to say that TF and DNA binding sites are complementary ($S_2$) is to say that certain kinds of chemical bonds can be formed ($B_1, B_2, \ldots, B_n$), which is why $S_2$ and $B_1, B_2, \ldots, B_n$ will be conceptually dependent. Finally, even if we could add different variables for each element of spatial and chemical-structural information, the characterization of $S_1, S_2, \ldots, S_n$ would remain very complex. This is due to the complexity of the shapes and spatial relations and to the large number of functional groups involved in the binding (cf. Rohs et al. 2010). The second modeling strategy thus encounters the same objections as the first: storing complex information into the characterization of the variables renders the causal model unmanageable and contradicts the basic assumption of causal graph theory that directed graphs that represent causal dependency relations are

![Fig. 3: Causal graph model M2 for protein-DNA recognition.](image-url)
central elements of causal models and thus are neither less informative nor bear less explanatory weight than the variables themselves.

To conclude, even if it might be in principle or technically possible to include information about complex spatial relations and chemical structures into a causal graph model, this can only be done at the expense of the adequacy of the causal model as it renders the causal model non-explanatory (because the information gets highly fragmented) and unmanageable and entails inconsistencies with basic assumptions of causal graph theory (namely, that variables must be conceptually independent and that causal dependency relations are central). Hence, the causal graph approach reaches its limits when it comes to explaining spatially-structurally complex biological phenomena.

7. Conclusions
I agree that causal modeling is central to scientific practice and that formal theories of causal modeling and explanation, such as causal graph theory, are powerful. However, I think that their significance is not universal and that it is important to also notice the limits of causal graph theory. In this paper, I have used an example from molecular biology to reveal one of these limitations: causal graph models fail to provide causal explanations of biological processes that involve complex spatial and chemical-structural relations.

My analysis of different modeling strategies has also shown why causal graph theory reaches its limits when trying to model cases such as protein-DNA recognition. One major obstacle is the huge extent and complexity of information about the parts of the involved molecules and their interactions that must be captured in the model. The other major obstacle is that there seems to be no way for a causal model to render intelligible the shapes of the two molecules, how they spatially fit together, and why this spatial fit enables certain other interactions to occur.
References


